

Ch 2: Measurement and Problem Solving

Exact numbers:

Measurements:



| <u>Team A:</u> | <u>Team B:</u> | <u>Team C:</u> |
|----------------|----------------|----------------|
| 5.6 cm         | 5.68 cm        | 5.49 cm        |
| 5.5 cm         | 5.66 cm        | 5.51 cm        |
| 5.4 cm         | 5.67 cm        | 5.50 cm        |

Averages:

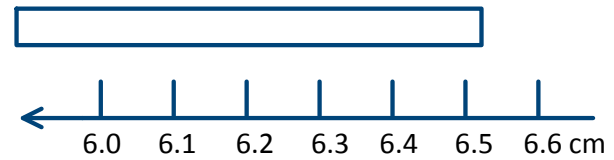
Quality of measurements:

Accuracy: "correctness" - how close to "true" value

Precision: "repeatability" - how close a group of values are to each other

Precision in measurements

Precision is usually dependent on how many marks are on the measuring device.



Every metric measurement has exactly one

Significant figures: used to track uncertainty through calculations

$$10.0 \text{ cm} / 3 =$$

## Significant figures

Which digits in a measurement are significant?

- All nonzero digits are significant
  - 23.48 cm
  - 1.22 cm
- Leading zeroes (to left of nonzero digits) are never significant
  - 0.00281 cm
  - 0.000281 cm
- Trapped zeroes (interior) are always significant
  - 0.002081 cm
  - 0.03002005 cm
- Trailing zeroes (to right of nonzero digits) are significant **IF** there's a decimal point anywhere in the measurement
  - 0.0050 cm
  - 48000.0 cm
  48000. cm
  - 48000 cm

## Rounding

Rounding reduces the number of sig figs in a measurement.

421.38 cm  $\xrightarrow[4 \text{ s.f.}]{\text{round to}}$

look at 1 digit to right of last sig fig:  
0-4 round down  
5-9 round up

922.248 cm  $\xrightarrow[4 \text{ s.f.}]{\text{round to}}$

5497 cm  $\xrightarrow[2 \text{ s.f.}]{\text{round to}}$

5497 cm  $\xrightarrow[3 \text{ s.f.}]{\text{round to}}$

Scientific notation

- Scientific notation:
- used to easily report very small or very large numbers
  - always clearly shows any desired number of significant figures (never ambiguous)

$$\# \times 10^{\square}$$

$10^0 =$   
 $10^1 =$   
 $10^2 =$   
 $10^3 =$

$2.00 \times 10^2 =$

$2.000 \times 10^2 =$

$5500 =$

Scientific notation

$9.78 \times 10^3$   $\xrightarrow{\text{decimal}}$

$1.34 \times 10^{-2}$   $\xrightarrow{\text{decimal}}$

$0.000\ 013\ 8$   $\xrightarrow{\text{sci}}$

## Entering scientific notation into a calculator

To use scientific notation on your calculator, you

must use the E EE or EXP key.

To enter  $1.38 \times 10^5$ :

To enter  $2.551 \times 10^{-3}$ :

text calculator:

numeric calculator:

## Sig figs in calculations

1. Multiplying or dividing:

- a. find the value with the fewest sig figs
- b. round answer to that number of sig figs

You travel 20.0 miles in 3.0 hours. What is your average speed in miles per hour?

$$100.00 \text{ cm} / 5 \text{ pieces} =$$

$$4.873 \times 10^2 \text{ cm} \times 9.2 \times 10^{-4} \text{ cm} =$$

Sig figs in calculations

2. Adding and subtracting:

- a. Find the value with the fewest number of decimal places (numbers to right of decimal point)
- b. Answer is rounded to that number of decimal places

$$142.1 \text{ cm} + 2.108 \text{ cm} + 28.32 \text{ cm} =$$

Answer limited by

Multiplying or  
dividing

Adding or  
subtracting

Combination calculations

Only round **once** at the end of a series of calculations!

Keep track of significance in intermediate calculations by underlining the last significant digit.

$$\begin{array}{r} 14.3 \text{ g} + 125 \text{ g} \\ \hline 1.3 \text{ cm} \times 2.86 \text{ cm} \end{array} =$$

On your own...

$$(17.236 - 17.1) \times (2.338 \times 1.53) =$$

## Measurement units

The **SI units** are a part of the metric system.

English system: feet, inches, pounds, etc.

### Basic SI units:

length: meter (m)

mass: kilogram (kg)

temp: kelvin (K)

**mass:** measure of the amount of matter present  
measured on a

**weight:** amount of gravitational force  
measured on a



kg (SI unit):

g (gram):

## SI prefixes

**SI prefixes** change the size of a unit by a power of 10

| prefix | abbrev. | power of 10 (definition)   |
|--------|---------|----------------------------|
| kilo   | k       | $10^3 = 1000$              |
| centi  | c       | $10^{-2} = 1/100 = 0.01$   |
| milli  | m       | $10^{-3} = 1/1000 = 0.001$ |

$$1 \text{ kg} = \text{___} \text{ g} = \text{___} \text{ g}$$

$$1 \text{ cm} = \text{___} \text{ m} = \text{___} \text{ m}$$

$$1 \text{ m} = \text{___} \text{ cm} = \text{___} \text{ cm}$$

$$1 \text{ mL} = \text{___} \text{ L} = \text{___} \text{ L}$$

$$1 \text{ L} = \text{___} \text{ mL} = \text{___} \text{ mL}$$

$$0.1234 \text{ m}$$

$$= \text{___} \text{ dm}$$

$$= \text{___} \text{ cm}$$

$$= \text{___} \text{ mm}$$

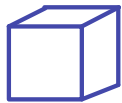
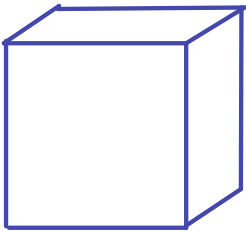
$$(d = 10^{-1})$$

$$c = 10^{-2}$$

$$m = 10^{-3}$$

## Volume

**Volume** is the amount of space occupied



## Dimensional analysis

**Dimensional analysis** is a process of unit conversion that works by cancelling unwanted units.

Say you're throwing a party. You prepare for:

15 guests

3 drinks per guest

In dimensional analysis, we use:

- 1 single given value to start with
- conversion factors
  - 2 units "per"
  - equation ( $2.54 \text{ cm} = 1 \text{ in}$ )

Start with the single value...

...then mult. by conversion factor fraction so original unit cancels.

Dimensional analysis

$$43.2 \text{ m} = ? \text{ cm}$$

remember...  
 $k = 10^3$   
 $c = 10^{-2}$   
 $m = 10^{-3}$

$$217 \text{ in} = ? \text{ km} \quad (\text{start with a roadmap})$$

Give the answer with the correct number of sig figs and in scientific notation.

Density

**Density** is the amount of mass per unit volume

$$D = \frac{\text{mass}}{\text{volume}}$$

An object has a mass of 14.3 g and a volume of 9.8 mL. What is its density?

Density is an **intensive property** (it does not depend on quantity.) So, it can be used to identify substances.

| <u>Substance</u> | <u>Density</u>          |
|------------------|-------------------------|
| gold             | 19.3 g/mL               |
| mercury          | 13.6 g/mL               |
| water            | 0.997 g/mL              |
| air              | 0.00130 g/mL = 1.30 g/L |



Density as a conversion factor

Density is **THE** conversion factor between mass and volume.

What volume Hg has a mass of 4.86 g?  
The density of Hg is 13.6 g/mL.

If you have 9.48 L Hg, what is its mass in grams?

Conversion practice

An object has a mass of 12.1 kilograms and a density of 4.5 g/mL. What is the volume of this object in fluid ounces? (1 fl oz = 29.57 mL)