

## Ch 2: Measurement and Problem Solving

Exact numbers: *Counting (or by definition)*

Measurements: *Contain some uncertainty*

length:



*marks every 0.1 cm*

	<u>Team A:</u>	<u>Team B:</u>	<u>Team C:</u>
<i>marks every 1 cm</i>	5. <u>6</u> cm	5.6 <u>8</u> cm	5.4 <u>9</u> cm
	5. <u>5</u> cm	5.6 <u>6</u> cm	5.5 <u>1</u> cm
	5. <u>4</u> cm	5.6 <u>7</u> cm	5.5 <u>0</u> cm
Averages:	<u>5.5 cm</u>	<u>5.67 cm</u>	<u>5.50 cm</u>

### Quality of measurements:

Accuracy: "correctness" - how close to "true" value

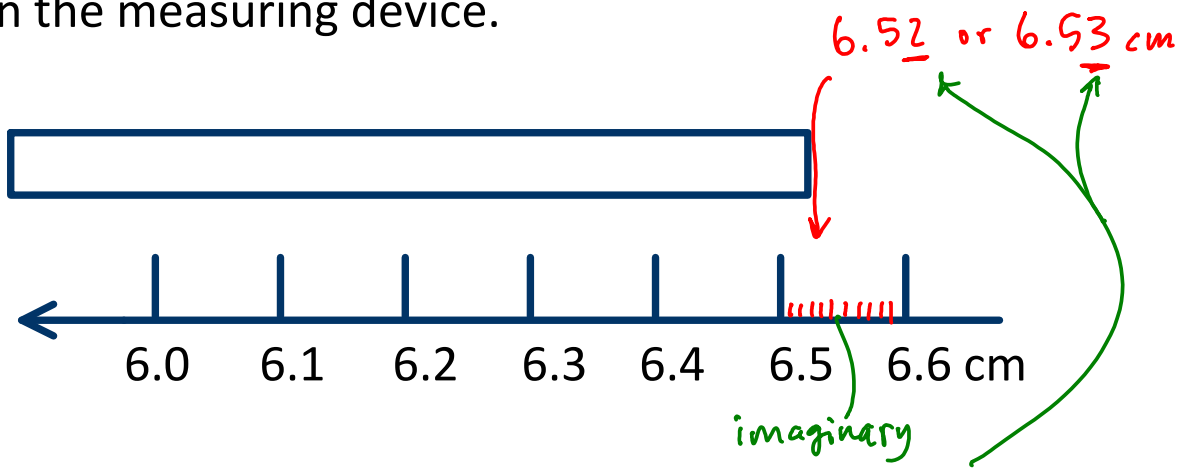
*A & C more accurate than B*

Precision: "repeatability" - how close a group of values are to each other

*B & C more precise than A*

## Precision in measurements

Precision is usually dependent on how many marks are on the measuring device.



Every metric measurement has exactly one uncertain digit.

Significant figures: used to track uncertainty through calculations

$$10.0 \text{ cm} / 3 = 3.33333 \dots \text{ cm}$$

too many digits!

## Significant figures

Which digits in a measurement are significant?

1. All nonzero digits are significant

a.  $\overset{\cdot}{2}\overset{\cdot}{3}.\overset{\cdot}{4}\overset{\cdot}{8}$  cm    4 sf.

b.  $\overset{\cdot}{1}.\overset{\cdot}{2}\overset{\cdot}{2}$  cm    3 sf

2. Leading zeroes (to left of nonzero digits) are never significant

a.  $0.00\overset{\cdot}{2}\overset{\cdot}{8}\overset{\cdot}{1}$  cm    3 sf

b.  $0.000\overset{\cdot}{2}\overset{\cdot}{8}\overset{\cdot}{1}$  cm    3 sf

3. Trapped zeroes (interior) are always significant

a.  $0.00\overset{\cdot}{2}\overset{\cdot}{0}\overset{\cdot}{8}\overset{\cdot}{1}$  cm    4 sf

b.  $0.0\overset{\cdot}{3}\overset{\cdot}{0}\overset{\cdot}{0}\overset{\cdot}{2}\overset{\cdot}{0}\overset{\cdot}{0}\overset{\cdot}{5}$  cm    7 sf

4. Trailing zeroes (to right of nonzero digits) are significant IF there's a decimal point anywhere in the measurement

a.  $0.00\overset{\cdot}{5}\overset{\cdot}{0}$  cm    2 sf

b.  $48\overset{\cdot}{0}\overset{\cdot}{0}\overset{\cdot}{0}.\overset{\cdot}{0}$  cm    6 sf

c.  $48\overset{\cdot}{0}\overset{\cdot}{0}\overset{\cdot}{0}\overset{\cdot}{0}$  cm    5 sf

d.  $\overset{(\cdot\cdot)}{48000}$  cm    unclear # sf. avoid this.  
(could assume worst - 2 sf only)

## Rounding

Rounding reduces the number of sig figs in a measurement.

$$\overset{\cdot}{4}\overset{\cdot}{2}\overset{\cdot}{1}.\overset{\cdot}{3}\overset{\cdot}{8} \text{ cm} \xrightarrow[4 \text{ s.f.}]{\text{round to}} \overset{\cdot}{4}\overset{\cdot}{2}\overset{\cdot}{1}.\overset{\cdot}{4} \text{ cm}$$

look at 1 digit to right of last sig fig:

0-4 round down

5-9 round up

$$\overset{\cdot}{9}\overset{\cdot}{2}\overset{\cdot}{2}.\overset{\cdot}{2}\overset{\cdot}{4}\overset{\cdot}{8} \text{ cm} \xrightarrow[4 \text{ s.f.}]{\text{round to}} \overset{\cdot}{9}\overset{\cdot}{2}\overset{\cdot}{2}.\overset{\cdot}{2} \text{ cm}$$

$$\overset{\cdot}{5}\overset{\cdot}{4}\overset{\cdot}{9}\overset{\cdot}{7} \text{ cm} \xrightarrow[2 \text{ s.f.}]{\text{round to}} \overset{\cdot}{5}\overset{\cdot}{5}\overset{\cdot}{0}\overset{\cdot}{0} \text{ cm}$$

$$\overset{\cdot}{5}\overset{\cdot}{4}\overset{\cdot}{9}\overset{\cdot}{7} \text{ cm} \xrightarrow[3 \text{ s.f.}]{\text{round to}} \overset{\cdot}{5}\overset{\cdot}{5}\overset{\cdot}{0}\overset{\cdot}{0} \text{ cm unclear}$$

~~$\overset{\cdot}{5}\overset{\cdot}{5}\overset{\cdot}{0}\overset{\cdot}{0}.$~~

must use scientific notation.

## Scientific notation

- Scientific notation:
- used to easily report very small or very large numbers
  - always clearly shows any desired number of significant figures (never ambiguous)

$$\underbrace{\#}_{\text{between 1-10}} \times \underbrace{10^{\square}}_{\substack{\text{power of 10} \\ \text{to change size}}}$$

$10^0 = 1$   
 $10^1 = 10$   
 $10^2 = 10 \times 10 = 100$   
 $10^3 = 1000$

$$\overset{\cdot}{2}.\overset{\cdot}{0}\overset{\cdot}{0} \times 10^2 = \overset{\cdot}{2}\overset{\cdot}{0}\overset{\cdot}{0}.$$

decimal      preserve 3 sig figs

$$\overset{\cdot}{2}\overset{\cdot}{0}\overset{\cdot}{0}\overset{\cdot}{0} \times 10^2 = \overset{\cdot}{2}\overset{\cdot}{0}\overset{\cdot}{0}.\overset{\cdot}{0} \quad 4 \text{ sf}$$

big #

$$\overset{\cdot}{5}\overset{\cdot}{5}\overset{\cdot}{0}\overset{\cdot}{0} = \overset{\cdot}{5}.\overset{\cdot}{5}\overset{\cdot}{0} \times \underbrace{10^3}$$

say we want 3 sf →

positive power of 10  
makes it a large #

## Scientific notation

$$9.78 \times 10^3 \xrightarrow{\text{decimal}} 9780$$

↑ placeholder

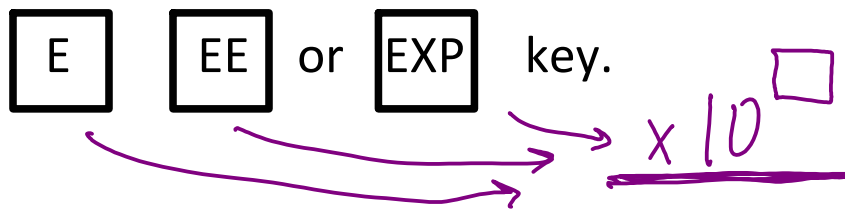
$$1.34 \times 10^{-2} \xrightarrow{\text{decimal}} 0.0134$$

$$0.0000138 \xrightarrow{\text{sci}} 1.38 \times 10^{-5}$$

## Entering scientific notation into a calculator

To use scientific notation on your calculator, you

must use the **E** **EE** or **EXP** key.



To enter  $1.38 \times 10^5$ :

1.38 **E** 5

To enter  $2.551 \times 10^{-3}$ :

text calculator:

numeric calculator: