

Announcements

Monday, October 19, 2009

Quiz 2 is this Wed, Oct 21 (ch 4 and most of 5)

MasteringChemistry due dates (all at 11:59pm)

- Ch 5: Fri, Oct 23
- Ch 6: Fri, Oct 30

Density of a gas

$$d = \frac{\text{mass}}{\text{volume}} = \frac{\text{molar mass}}{\text{molar volume}} \quad \text{periodic table (g/mol)} \quad 22.4 \text{ L/mol at STP}$$

(g/L) for gases

What is the density of oxygen gas at STP? O₂ (g)

$$M_m \text{ O}_2 = 32.00 \text{ g/mol}$$

molar volume
of any gas = 22.4 L/mol
at STP

$$d = \frac{32.00 \text{ g/mol}}{22.4 \text{ L/mol}} = \boxed{1.43 \text{ g/L}} \text{ at STP}$$

$$\text{SF}_6 \quad \text{sulfur hexafluoride} \quad d \text{ at STP} = \frac{146.07 \text{ g/mol}}{22.4 \text{ L/mol}} = \boxed{6.52 \text{ g/L}}$$

At other pressures or temperatures... $PV = nRT$

$$n = \frac{m(g)}{M_m} \times \frac{1 \text{ mol}}{M_m} \quad n = \frac{m}{M_m}$$

$$PV = \frac{m}{M_m} RT \rightarrow PM_m = \frac{m}{V} RT \rightarrow \boxed{PM_m = dRT}$$

What is the density of O₂(g) at 125 °C and 740 mmHg?

$$d = \frac{PM_m}{RT} = \frac{(0.97368 \text{ atm})(32.00 \text{ g/mol})}{(0.08206 \frac{\text{L} \cdot \text{atm}}{\text{K} \cdot \text{mol}})(398.15 \text{ K})} = \boxed{0.954 \text{ g/L}}$$

$$P = 740 \text{ mmHg} \times \frac{1 \text{ atm}}{760 \text{ mmHg}} = 0.97368 \text{ atm}$$

$$M_m = 32.00 \text{ g/mol}$$

$$R = 0.08206 \frac{\text{L} \cdot \text{atm}}{\text{K} \cdot \text{mol}}$$

$$T = 125^\circ\text{C} + 273.15 = 398.15 \text{ K}$$

Molar mass of a gas

Given: mass, volume, pressure, temperature

Calculate: molar mass (g/mol) $d = m/v$

$$PM_m = dRT \quad M_m = \frac{dRT}{P} = \frac{mRT}{VP}$$

Calculate the molar mass of a gas sample with mass of 0.582 g, volume of 213 mL, pressure of 754 mmHg, and temperature of 100.0 °C.

$$M_m = \frac{mRT}{VP} = \frac{(0.582 \text{ g}) \left(0.08206 \frac{\text{L} \cdot \text{atm}}{\text{K} \cdot \text{mol}}\right) (373.15 \text{ K})}{(0.213 \text{ L}) (0.9921 \text{ atm})}$$

$$m = 0.582 \text{ g}$$

$$R = 0.08206 \frac{\text{L} \cdot \text{atm}}{\text{K} \cdot \text{mol}}$$

$$T = 100.0^\circ\text{C} + 273.15 = 373.15 \text{ K}$$

$$V = 213 \text{ mL} \times \frac{1 \text{ L}}{1000 \text{ mL}} = 0.213 \text{ L}$$

$$P = 754 \text{ mmHg} \times \frac{1 \text{ atm}}{760 \text{ mmHg}} = 0.9921 \text{ atm}$$

$$= \boxed{84.3 \text{ g/mol}}$$

Mixtures of gases

Gas molecules act independently!

For any mixture of gases, the total pressure is the sum of the pressures that each gas exerts (partial pressures)

$P_{\text{total}} = P_a + P_b + P_c + \dots$ (Dalton's law of partial pressures)

$$\text{Mole fraction} = \frac{n_a}{n_{\text{total}}} = \chi_a \quad \text{for 1 substance} \quad \text{greek chi} \quad \chi$$

In one container with constant V and T ,

$$\frac{n_a}{n_{\text{total}}} = \frac{P_a}{P_{\text{total}}} = \chi_a \quad \text{Mole fraction of "a"} \quad P_a = \chi_a P_{\text{total}} \quad \text{Partial pressure of "a"}$$

Air is 78% nitrogen by volume. What is the partial pressure of nitrogen if the atmospheric pressure is 755 mmHg that day?

$$\chi_{N_2} = 0.78 \quad (78\% \text{ by volume})$$

$$P_{N_2} = (\chi_{N_2}) (P_{\text{tot}}) = (0.78) (755 \text{ mmHg})$$

(partial pressure of N_2)

$$= \boxed{590 \text{ mmHg}}$$

Mole fraction and partial pressure

A mixture of 5 g H_2 , 8 g N_2 , and 10 g O_2 has a total pressure of 7 atm. What is P_{H_2} , P_{N_2} , and P_{O_2} ?

$$5 \text{ g } H_2 \times \frac{1 \text{ mol } H_2}{2.016 \text{ g } H_2} = 2.480 \text{ mol } H_2$$

$$8 \text{ g } N_2 \times \frac{1 \text{ mol } N_2}{28.02 \text{ g } N_2} = 0.2855 \text{ mol } N_2$$

$$10 \text{ g } O_2 \times \frac{1 \text{ mol } O_2}{32.00 \text{ g } O_2} = 0.3125 \text{ mol } O_2$$

$$\Sigma = 3.078 \text{ mol total}$$

$$X_{H_2} = \frac{2.480 \text{ mol } H_2}{3.078 \text{ mol tot}} = 0.8057$$

$$X_{N_2} = \frac{0.2855 \text{ mol } N_2}{3.078 \text{ mol tot}} = 0.09276$$

$$X_{O_2} = \frac{0.3125 \text{ mol } O_2}{3.078 \text{ mol tot}} = 0.1013$$

$$P_{H_2} = (0.8057)(7 \text{ atm}) = 6 \text{ atm}$$

$$P_{N_2} = (0.09276)(7 \text{ atm}) = 0.6 \text{ atm}$$

$$P_{O_2} = (0.1013)(7 \text{ atm}) = 0.7 \text{ atm}$$

What is the volume of this container if $T = 298 \text{ K}$?

$$PV = nRT \quad V = \frac{nRT}{P} \quad \text{use total for } n \text{ and } P$$

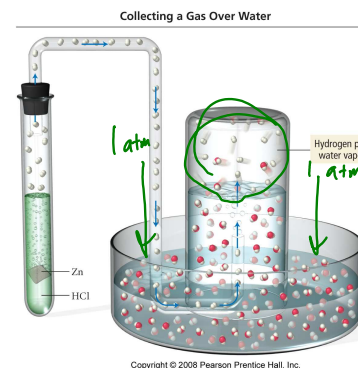
$$V = \frac{(3.078 \text{ mol})(0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}})(298 \text{ K})}{(7 \text{ atm})} = 10.75 \text{ L} \rightarrow 10 \text{ L}$$

Collecting a gas over water

Partial pressures work in the ideal gas law too...

$$P_a V = n_a RT \text{ for one gas (a) in a mixture of gases}$$

Collection of a gas over water



When H_2 is produced by the reaction, the gas collected is a mixture of H_2 and water vapor.

Vapor pressure of water:

max P_{H_2O} when a gas is saturated with water vapor

T P_{H_2O} (mmHg)

20 °C 17.55

23 °C 21.10

25 °C 23.78

$$P_{\text{total}} = P_{H_2O} + P_{H_2}$$

atmospheric pressure (barometer) vapor pressure of H_2O

use in $PV = nRT$ to calc mol $H_2(g)$

Collecting gases over water

If you collect 19.0 mL of gas over water from a reaction that produces $\text{H}_2(g)$, how many moles of hydrogen gas were collected? Atmospheric pressure = 760 mmHg, $T = 23^\circ\text{C}$.

$$P_{\text{tot}} = P_{\text{H}_2\text{O}} + P_{\text{H}_2}$$

(correcting for vapor
pressure of H_2O)

$$P_{\text{tot}} = 760 \text{ mmHg}$$

$$P_{\text{H}_2\text{O}(g)} = 21.10 \text{ mmHg}$$

$$P_{\text{H}_2} = P_{\text{tot}} - P_{\text{H}_2\text{O}}$$

corrected

$$P_{\text{H}_2} V = n_{\text{H}_2} RT$$

$$n_{\text{H}_2} = \underline{\hspace{2cm}}$$

$$P_{\text{H}_2} =$$

$$V =$$

$$R =$$

$$T =$$

at STP and ignoring H_2O vapor...