

Topic

RLC Circuits

Governing Equations and Assumptions

$$\begin{aligned}
 v(t) &= A_1 e^{s_1 t} + A_2 e^{s_2 t} & \alpha &= \frac{1}{2RC} \\
 s_{1,2} &= -\alpha \pm \sqrt{\alpha^2 - \omega_0^2} & \omega_0 &= \frac{1}{\sqrt{LC}} \quad \left. \vphantom{\begin{aligned} \alpha &= \frac{1}{2RC} \\ \omega_0 &= \frac{1}{\sqrt{LC}} \end{aligned}} \right\} \text{Parallel RLC Circuit} \\
 i(t) &= A_1 e^{s_1 t} + A_2 e^{s_2 t} & \alpha &= \frac{R}{2L} \\
 s_{1,2} &= -\alpha \pm \sqrt{\alpha^2 - \omega_0^2} & \omega_0 &= \frac{1}{\sqrt{LC}} \quad \left. \vphantom{\begin{aligned} \alpha &= \frac{R}{2L} \\ \omega_0 &= \frac{1}{\sqrt{LC}} \end{aligned}} \right\} \text{Series RLC Circuit}
 \end{aligned}$$

Process

- ① Determine the Damping
Compare α^2 & ω_0^2
 $\omega_0^2 < \alpha^2 \Rightarrow$ Overdamped
 $\omega_0^2 > \alpha^2 \Rightarrow$ Underdamped
 $\omega_0^2 = \alpha^2 \Rightarrow$ Critically Damped
- ② Apply the correct $v(t)$ or $i(t)$ expression based on the damping
- ③ Determine the constants

$$\begin{aligned}
 v(0^+) &= V_0 \\
 \frac{dv(0^+)}{dt} &= -\frac{I_0}{C} - \frac{V_0}{RC} \quad \left. \vphantom{\begin{aligned} v(0^+) &= V_0 \\ \frac{dv(0^+)}{dt} &= -\frac{I_0}{C} - \frac{V_0}{RC} \end{aligned}} \right\} \text{Parallel} \\
 i(0^+) &= I_0 \\
 \frac{di(0^+)}{dt} &= -\frac{I_0 R}{L} - \frac{V_0}{L} \quad \left. \vphantom{\begin{aligned} i(0^+) &= I_0 \\ \frac{di(0^+)}{dt} &= -\frac{I_0 R}{L} - \frac{V_0}{L} \end{aligned}} \right\} \text{Series}
 \end{aligned}$$
- ④ If needed, solve for other quantities

$$\text{Parallel} \quad i_R(t) = \frac{v(t)}{R}, \quad i_C(t) = C \frac{dv}{dt}, \quad i_L(t) = -i_R(t) - i_C(t)$$

$$\text{Series} \quad v_R(t) = i(t)R, \quad v_L(t) = L \frac{di}{dt}, \quad v_C(t) = -v_R(t) - v_L(t)$$