

8.2

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10:58 AM

Properties of Radicals

Assume we are always in the reals. (ie no even roots of neg. no dividing by zero)

multiplication of radicals

$$\sqrt{ab} = \sqrt{a} \sqrt{b}$$

ex) $\sqrt{9 \cdot 4} = \sqrt{9} \cdot \sqrt{4}$

$$\sqrt{9} \cdot \sqrt{4} = 3 \cdot 2 = 6$$

ex) $\sqrt{25x} = \sqrt{25} \sqrt{x} = 5\sqrt{x}$

ex) $\sqrt{3x} \sqrt{2y} = \sqrt{6xy}$

note: this is NOT true for add/subst.

ex) $\sqrt{9} + \sqrt{4} \neq \sqrt{9+4}$

$$3 + 2 \neq \sqrt{13}$$

$$5 \neq \sqrt{13}$$

Division of radicals

$$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$$

ex) $\sqrt{\frac{1}{4}} = \frac{\sqrt{1}}{\sqrt{4}} = \frac{1}{2}$

$$\sqrt{\frac{x}{16}} = \frac{\sqrt{x}}{\sqrt{16}} = \frac{\sqrt{x}}{4}$$

$$\frac{\sqrt{32x^3}}{\sqrt{2x}} = \sqrt{\frac{32x^3}{2x}} = \sqrt{16x^2} = \sqrt{16} \sqrt{x^2} = 4x$$

Simplifying Radical Expressions

A radical is simplified when

All Powers in radicand are less than the index
(factor out whatever you can)

(ex.) Simplify. $\sqrt{20} = \sqrt{4 \cdot 5} = \sqrt{4} \cdot \sqrt{5} = 2\sqrt{5}$

~~$\sqrt{2 \cdot 10}$~~

$$\sqrt[3]{40} = \sqrt[3]{8 \cdot 5} = \sqrt[3]{8} \sqrt[3]{5} = 2\sqrt[3]{5}$$

$$\begin{aligned} \sqrt{200} &= \sqrt{100 \cdot 2} = \sqrt{100} \sqrt{2} = 10\sqrt{2} \\ \sqrt{20 \cdot 10} &= \sqrt{4 \cdot 5 \cdot 10} = \sqrt{4} \sqrt{5} \sqrt{10} = 2\sqrt{5} \sqrt{10} = 2\sqrt{5 \cdot 10} = 2\sqrt{50} \\ &= 2\sqrt{25 \cdot 2} = 2 \cdot 5\sqrt{2} = 10\sqrt{2} \end{aligned}$$

$$\begin{aligned} \sqrt{x^{17}} &= \sqrt{x^{16} \cdot x} \\ &= \sqrt{(x^8)^2 \cdot x} = \sqrt{(x^8)^2} \sqrt{x} = x^8 \sqrt{x} \end{aligned}$$

$$\sqrt{162x^5} =$$

$$\begin{aligned} \sqrt{81 \cdot 2 \cdot x^5} &= \sqrt{81} \sqrt{2x^5} = 9\sqrt{2x^5} \\ &= 9\sqrt{2x^4 \cdot x} = 9\sqrt{2(x^2)^2 \cdot x} \\ &= 9\sqrt{(x^2)^2} \sqrt{2x} \\ &= 9x^2 \sqrt{2x} \end{aligned}$$