

7.3

C.I. for Mean (σ unknown & $n < 30$)
Using Calculator

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Confidence Intervals for the Mean (σ unknown & $n < 30$)

When σ is unknown and $n < 30$ we can't use normal to find C.I., we must use t distribution.

Characteristics of t -dist.

1. bell-shaped
2. Symmetric about mean
3. mean = median = mode = 0
4. Never touches x -axis

1. Variance > 1

2. t -dist. is a group of curves based on "degrees of freedom"

3. as $n \rightarrow \infty$, t -dist \rightarrow normal.

degrees of freedom, d.f. - the number of values that are free to vary after a sample statistic has been computed.

⊗ I have 8 numbers, mean = 5, the sum of the #'s must be 40 (since $\frac{40}{8} = 5$). So the first 7 numbers can be anything but the 8th number must make the sum 40. So 7 d.f.

So for right now d.f. = $n - 1$ (for C.I.)

Formula for C.I. for mean when σ is unknown & $n < 30$

$$\bar{X} - t_{\alpha/2} \left(\frac{S}{\sqrt{n}} \right) < \mu < \bar{X} + t_{\alpha/2} \left(\frac{S}{\sqrt{n}} \right)$$

The $df. = n - 1$

① ex 1 sample 10 students about age. $\bar{X} = 20$
 $S = 1$. Find 90% C.I. for the mean age.

$$\bar{X} = 20, \alpha = .10, \alpha/2 = .05 \quad S = 1 \quad n = 10 \quad df. = 9$$

$$20 - 1.833 \left(\frac{1}{\sqrt{10}} \right) < \mu < 20 + 1.833 \left(\frac{1}{\sqrt{10}} \right)$$

$$19.42 < \mu < 20.58$$

t-dist on pg. 731

Using Your Calculator

Data

1. Enter L_1
2. STAT \rightarrow TESTS \rightarrow 8-tInterval
3. DATA
4. Enter stuff
5. Calculate

Stats

1. STAT \rightarrow TESTS \rightarrow 8-tInterval
2. Stats
3. Enter stuff
4. Calculate