

2.6

Interval Notation

We use interval notation for short

(a) is used for $< a >$ (called exclusive)
 $[a]$ is used for $\leq a \geq$ (called inclusive)

ex $2 < x < 10 \rightarrow (2, 10)$

▪ $2 \leq x \leq 10 \rightarrow [2, 10]$

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$2 \leq x < 10 \rightarrow [2, 10)$

ex $x > -5 \rightarrow (-5, \infty)$, ∞ represents infinity

▪ $x \leq -5 \rightarrow (-\infty, -5]$

We never "include" ∞ or $-\infty$, that is don't write $[-\infty$ or $\infty]$.

Graphing Inequalities

⊗ $x > 3$ $\leftarrow \begin{array}{c} | \\ 0 \end{array} \begin{array}{c} | \\ 1 \end{array} \begin{array}{c} | \\ 2 \end{array} \begin{array}{c} | \\ 3 \end{array} \rightarrow$ or $\leftarrow \begin{array}{c} | \\ 0 \end{array} \begin{array}{c} | \\ 1 \end{array} \begin{array}{c} | \\ 2 \end{array} \begin{array}{c} | \\ 3 \end{array} \rightarrow$

■ $x \geq 3$ $\leftarrow \begin{array}{c} | \\ 0 \end{array} \begin{array}{c} | \\ 1 \end{array} \begin{array}{c} | \\ 2 \end{array} \begin{array}{c} | \\ 3 \end{array} \rightarrow$ or $\leftarrow \begin{array}{c} | \\ 1 \end{array} \begin{array}{c} | \\ 2 \end{array} \begin{array}{c} | \\ 3 \end{array} \rightarrow$

⊗ $1 < x < 3$ $\leftarrow \begin{array}{c} | \\ 0 \end{array} \begin{array}{c} | \\ 1 \end{array} \begin{array}{c} | \\ 2 \end{array} \begin{array}{c} | \\ 3 \end{array} \rightarrow$ or $\leftarrow \begin{array}{c} | \\ 0 \end{array} \begin{array}{c} | \\ 1 \end{array} \begin{array}{c} | \\ 2 \end{array} \begin{array}{c} | \\ 3 \end{array} \rightarrow$

■ $1 \leq x < 3$ $\leftarrow \begin{array}{c} | \\ 0 \end{array} \begin{array}{c} | \\ 1 \end{array} \begin{array}{c} | \\ 2 \end{array} \begin{array}{c} | \\ 3 \end{array} \rightarrow$ or $\leftarrow \begin{array}{c} | \\ 0 \end{array} \begin{array}{c} | \\ 1 \end{array} \begin{array}{c} | \\ 2 \end{array} \begin{array}{c} | \\ 3 \end{array} \rightarrow$

Solving Inequalities

Solution of an inequality - any number that makes an inequality true

ex) $x < 5$; 2 is a solution, so is 3, 4, 1, 0, -1, -2, ...

To solve for complicated inequalities

If $a < b$ then $a + c < b + c$ (same w/ $a \leq b, a > b, a \geq b$)

If $a < b$ then $a - c < b - c$ "

ex) $x + 2 \leq 5$
 $\quad \quad \quad -2 \quad -2$

▪ $x \leq 3$

try a couple: $0 + 2 = 2 \leq 5$

$4 + 2 = 6 \not\leq 5$

ex) $x - 10 > -5$
 $\quad \quad \quad +10 \quad +10$

▪ $x > 5$

try a couple: $6 - 10 = -4 > -5$

$4 - 10 = -6 \not> -5$

Multiplication/division for inequalities is different

If $a < b$ and c is positive, then $ac < bc$

If $a < b$ and c is negative, then $ac > bc$

Same true for $\frac{a}{c} < \frac{b}{c}, \frac{a}{c} > \frac{b}{c}$

Same true for $>, \leq, \geq$

This says, if \times or \div by a negative number, switch the sign.

\leq and \geq , $<$ and $>$

$$\textcircled{\text{ex}} \frac{x}{-5} > 2$$

$$-5\left(\frac{x}{-5}\right) < -5(2)$$

$$x < -10$$

$$\text{try a couple: } \frac{-15}{-5} = 3 > 2$$

$$\frac{0}{-5} = 0 \not> 2$$

$$-3x \leq 6$$

$$\frac{-3x}{-3} \geq \frac{6}{-3}$$

$$x \geq -2$$

$$\text{try a couple: } -3(0) = 0 \leq 6$$

$$-3(-3) = 9 \not\leq 6$$

$$\textcircled{\text{ex}} \begin{array}{r} 5x - 2 < 8 \\ +2 \quad +2 \end{array}$$

$$5x < 10$$

$$x < 2$$

$$-3x + 4 \geq 13$$

$$-3x \geq 9$$

$$x \leq -3$$

$$\frac{2x+4}{-3} \leq -4$$

$$2x+4 \geq 12$$

$$2x \geq 8$$

$$x \geq 4$$

try a couple:

$$5(1) - 2 = 3 < 8 \checkmark$$

$$5(3) - 2 = 13 < 2 \checkmark$$

$$-3(-4) + 4 = 16 \geq 13$$

$$-3(-2) + 4 = 10 \not\geq 13$$

$$\frac{2(5)+4}{-3} = \frac{14}{-3} = -4.\bar{6} \leq -4$$

$$\frac{2(3)+4}{-3} = \frac{10}{-3} = -3.\bar{3} \not\leq -4$$

$$\textcircled{\text{ex}} 3(x+7) - 15 > 4(x-2)$$

$$3x + 21 - 15 > 4x - 8$$

$$3x + 6 > 4x - 8$$

$$14 > x \text{ or } x < 14$$

try a couple:

$$3(13+7) - 15 = 60 - 15 = 45 \checkmark$$

$$4(13-2) = 4(11) = 44$$